

Part A

(1)

$$f(x) = 2x + a$$

$$g(x) = ax + 3$$

$$fg(x) = 10x + b$$

where 'a' and 'b' are constants

work out the values of 'a' and 'b'

(2)

$$f(x) = dx - e$$

$$g(x) = ex - 1$$

$$fg(x) = 18x - 11$$

where 'd' and 'e' are constants

work out the values of 'd' and 'e'

(3)

$$f(x) = hx + k$$

$$g(x) = kx + h$$

$$fg(x) = 20x + 14$$

where 'k' and 'h' are constants

work out the values of 'k' and 'h'

(4)

$$f(x) = mx - n$$

$$g(x) = nx + m$$

$$gf(x) = 12x - 13$$

where 'm' and 'n' are constants

work out the values of 'm' and 'n'

(5)

$$f(x) = vx + w$$

$$g(x) = 2vx + 2w$$

$$gf(x) = 18x + 16$$

work out two values for each of 'v' and 'w'

(6)

$$f(x) = 2x + p$$

$$g(x) = px + 3$$

$$gf(x) = 2px + 5p - 1$$

work out two values for 'p'

Part B

Show that $fg(x) = gf(x)$ for each of the following cases.

(1)

$$f(x) = 3x + 2$$

$$g(x) = 6x + 5$$

(2)

$$f(x) = 1\frac{1}{2}x + 6$$

$$g(x) = 1\frac{1}{4}x + 3$$

Part C

In general: $f(x) = ax + b$

$$g(x) = cx + d$$

where a , b , c and d are constants, what relationship is there between the four constants if $fg(x) = gf(x)$?

Can you make up some further examples and test whether your rule works?